Characterizing CMIP5 model spread in simulated rainfall in the Pacific Intertropical Convergence and South Pacific Convergence Zones

Benjamin R. Lintner1, Baird Langenbrunner2, J. David Neelin2, Bruce T. Anderson3, Matthew J. Niznik4, Gen Li5, and Shang-Ping Xie6

1Department of Environmental Sciences, Rutgers, The State University of New Jersey, New Brunswick, New Jersey, USA, 2Department of Atmospheric and Oceanic Sciences, University of California, Los Angeles, California, USA, 3Department of Earth and Environment, Boston University, Boston, Massachusetts, USA, 4Rosenstiel School of Marine and Atmospheric Sciences, University of Miami, Coral Gables, Florida, USA, 5State Key Laboratory of Tropical Oceanography, South China Sea Institute of Oceanology, Chinese Academy of Sciences, Guangzhou, China, 6Scripps Institution of Oceanography, La Jolla, California, USA

Abstract
Current-generation climate models exhibit various errors or biases in both the spatial distribution and intensity of precipitation relative to observations. In this study, empirical orthogonal function analysis is applied to the space-model index domain of precipitation over the Pacific from Coupled Model Intercomparison Project Phase 5 (CMIP5) simulations to explore systematic spread of simulated precipitation characteristics across the ensemble. Two significant modes of spread, generically termed principal uncertainty patterns (PUPs), are identified in the December-January-February precipitation climatology: the leading PUP is associated with the meridional width of deep convection, while the second is associated with tradeoffs in precipitation intensity along the South Pacific Convergence Zone, the Intertropical Convergence Zone (ITCZ), and the spurious Southern Hemisphere ITCZ. An important factor distinguishing PUPs from the analogy to time series analysis is that the modes can reflect either true systematic intermodel variance patterns or internal variability. In order to establish that the PUPS reflect the former, three complementary tests are performed by using preindustrial control simulations: a bootstrap significance test for reproducibility of the intermodel spatial patterns, a check for robustness over very long climatological averages, and a test on the loadings of these patterns relative to interdecadal sampling. Composite analysis based on these PUPs demonstrates physically plausible relationships to CMIP5 ensemble spread in simulated sea surface temperatures (SSTs), circulation, and moisture. Further analysis of atmosphere-only, prescribed SST simulations demonstrates decreased spread in the spatial distribution of precipitation, while substantial spread in intensity remains.

1. Introduction
The tropical Pacific as simulated by state-of-the-art global climate models, including those in Phase 5 of the Coupled Model Intercomparison Project (CMIP5), is characterized by several well-known biases. Prominent among these are the eastern Pacific cold-tongue bias, with colder than observed sea surface temperatures (SSTs) frequently confined too close to the equator and penetrating too far to the west [Zheng et al., 2012; Li et al., 2015], and the double Intertropical Convergence Zone (ITCZ), with two bands of deep convection in the east, one on either side of the equator, rather than the observed equatorially asymmetric state with deep convection confined to the Northern Hemisphere only [Mechoso et al., 1995; Li et al., 2004; Lin, 2007]. Among the hypotheses accounting for the genesis of biases or errors in eastern tropical Pacific climate are deficiencies in the representation of coupled ocean-atmosphere features or processes, such as spurious warming in the upwelling zone along the South American coast and too strong surface winds and ocean currents [Zheng et al., 2012] or larger-scale issues related to hemispheric energy imbalances [Hwang and Frierson, 2013]. Intermodel differences in parameterizations of deep convection as well as clouds, especially low-level marine stratocumuli, may further contribute to errors in simulation of tropical Pacific climate in current generation models [Mechoso et al., 1995; Zhang 2001; Lin, 2007; Brown et al., 2013].

Perhaps less well appreciated are the biases occurring outside of the eastern tropical Pacific, particularly those in and around the South Pacific Convergence Zone (SPCZ), a diagonally oriented convection zone extending from the tropical western Pacific warm pool southeastward into the Southern Hemisphere (SH)
midlatitudes of the central Pacific [Vincent, 1994]. Coupled models frequently produce SPCZs that are more zonal than observed and with precipitating deep convection penetrating too far into the southeast Pacific dry descent region [Brown et al., 2011, 2012; Ganachaud et al., 2014] (see also Figure 1). Niznik et al. [2015] stress the importance of distinguishing between the tropical and subtropical portions of the SPCZ when analyzing model bias, given the distinct processes influencing the tropical and subtropical portions. In light of the biases in the eastern equatorial Pacific, it is of interest to quantify how these may affect, or in turn be affected by, the biases in the SPCZ. Moreover, to the extent that biases reflect linkages among components of the climate system, their diagnosis may contribute to understanding why the SPCZ exists, as this remains elusive [Takahashi and Battisti, 2007; Power, 2011].

It is noteworthy that the aforementioned biases are little improved from the CMIP3 to CMIP5 model ensembles [Hirota et al., 2011; Li and Xie, 2012; Brown et al., 2012; Hirota and Takayabu, 2013; Li and Xie, 2014]. The continuing occurrence of substantial biases in simulations of present-day climate limits confidence in projections of anthropogenic climate change impacts, especially at the regional scales considered for mitigation and adaptation [Intergovernmental Panel on Climate Change, 2013]. For example, Widlansky et al. [2013] document substantial change in SPCZ region precipitation under future warming, including an equatorward shift of the mean SPCZ axis with amplified 21st century surface warming in the eastern Pacific. For many islands in the Pacific that depend on precipitation from the SPCZ, such shifts would clearly impact water resources and infrastructure, but the errors existing in current climate simulation need to be resolved to meet the needs of planning and decision making.
An outstanding challenge in model intercomparison, assessment, and validation involves quantifying what may be a range of simulated behaviors across model ensembles. A common approach involves quantifying biases or errors in terms of the model ensemble mean (MEM) and some bulk measure of the spread across the ensemble, e.g., the intermodel standard deviation or root-mean-square difference with respect to the MEM. However, such metrics may fall short of capturing how the models differ with respect to one another. Our perspective is that the study of systematic differences across a model ensemble may ultimately help to isolate deficiencies in model physics and suggest targets for improvement, beyond what biases or errors in the MEM may already indicate about model deficiencies and how to resolve them. Certainly, in light of the wide array of physical implementations and parameterizations and associated tunable parameters used in current generation models, determining precisely how to correct a particular error may be challenging. Nevertheless, we suggest that the application of methodologies to identify spread in models is useful: at the very least, objective grouping of models based on shared structural features can guide the selection of models for specific applications, such as the design of a multimodel ensemble. As we show below, the methodology we apply here highlights the tendency for models of the same “family” to behave similarly. To the extent that we can consider such similar behavior as reflecting nonindependence across these models, one may choose to include only a single representative of a family in an ensemble.

To quantify the spread in simulation of climatological precipitation in the CMIP5 ensemble, we consider here the application of objective empirical mode decomposition techniques to the entire model suite. In the present study, we apply empirical orthogonal function/principal component (EOF/PC) analysis on the space-model index domain rather than the conventional space-time domain. This approach, which we generically term principal uncertainty pattern (PUP) analysis regardless of the specific decomposition technique used, is conceptually similar to recent studies by, e.g., Deser et al. [2012], regarding internal variability in a single model ensemble; Delcambre et al. [2013a, 2013b]; regarding the Northern Hemisphere jet in the CMIP3 archive; and Li and Xie [2012, 2014, with the latter referred to hereinafter as LX14] regarding tropics-wide SST in CMIP3/CMIP5 and tropical Pacific precipitation biases in CMIP5. More recently, Anderson et al. [2015] performed a multivariate PUP analysis to relate CMIP5-simulated trends in SST to trends in land surface precipitation, while Langenbrunner et al. [2015] applied PUP analysis to identify and attribute CMIP5 model discrepancies in the simulated meridional position and longitudinal extent of the North Pacific storm track in current climate as well as end of the 21st century projections.

2. Data and Methods

We seek here to characterize CMIP5 model spread in simulations of rainfall in the tropical Pacific, focusing primarily on the austral summer (December-January-February or DJF) season, when the SPCZ is most prominent. In order to address the impact of coupled ocean-atmosphere versus atmosphere-only sources of model spread, we analyze both the historic (coupled) simulations of CMIP5 as well as stand-alone atmospheric models forced with prescribed sea surface temperature and sea ice boundary conditions [Taylor et al., 2012]. The latter follow a protocol similar to the Atmospheric Model Intercomparison Project (AMIP) and are thus referred to hereafter as AMIP-style simulations. For the historic suite, 36 models are analyzed; for the AMIP-style suite, 30 models are analyzed. The models and associated acronyms are summarized in Table 1. For each available model, we use only a single ensemble member to give equal weighting to each model in the analysis. For ease of comparison, all model fields are first regridded by using bilinear interpolation to a uniform 2.5° × 2.5° grid over a rectangular domain spanning 120°E–60°W and 50°S–20°N. For both the historic and AMIP-style simulations, 27 years of data for DJF are analyzed, spanning the common period of 1979–2005. Of course, the AMIP simulations are forced with observed SSTs while the historic simulations have SSTs that freely evolve subject to prescribed forcings from insolation, volcanic eruptions, and anthropogenic emissions. As we elaborate on further below, the behavior we identify is robust to the sampling time period.

Precipitation climatologies for both the coupled and AMIP-style ensembles are concatenated to form $M \times N$ matrices, where $M$ denotes the spatial dimension (i.e., $M = Mx \times My$ longitude-latitude points) and $N$ denotes the model index dimension; EOFs and PCs are computed from each $M \times N$ matrix. The resulting modes (or PUPs) capture the leading spatial patterns of intermodel differences in terms of variance explained across the space-model index domain. The PC associated with each PUP corresponds to the loadings (or projections) of individual model climatologies onto that spatial pattern (EOF), providing an indication of the relative contribution of
each model to that PUP. For example, a large positive loading or PC value for a given model means that it projects strongly (and positively) onto that mode, relative to the ensemble mean. These weights are further used as the basis for regression analysis of various fields related to precipitation, including SST, winds, and moisture.

We have also applied maximum covariance analysis (MCA) to the cross-covariance matrix of precipitation and SST. The MCA-based approach yields pairs of uncertainty patterns for precipitation and SST representing coupled ensemble spread in these two fields. For more information on these methods, the reader is referred to Langenbrunner et al. [2015, and references therein].

3. Results
3.1. PUPs for Coupled Model Simulations

In computing the PUPs, we seek to identify systematic variation in model behavior relative to the MEM. Thus, for reference, Figure 1 shows DJF MEM precipitation for the historic simulations as well as the departure of

Table 1. List of Model Centers/Groups and Associated Acronyms of the Models Analyzed

<table>
<thead>
<tr>
<th>Modeling Center/Group/Country</th>
<th>Historic Ensemble Acronym</th>
<th>Preindustrial Control Length (years)</th>
<th>AMIP-Ensemble Acronym</th>
</tr>
</thead>
<tbody>
<tr>
<td>Commonwealth Scientific and Industrial Research Organisation (CSIRO) and Bureau of Meteorology (BOM), Australia</td>
<td>ACCESS1-0</td>
<td>500</td>
<td>ACCESS1-0</td>
</tr>
<tr>
<td>Beijing Climate Center, China Meteorological Administration</td>
<td>ACCESS1-3</td>
<td>500</td>
<td>ACCESS1-3</td>
</tr>
<tr>
<td>bcc-cesm1-1</td>
<td>400</td>
<td>bcc-cesm1-1</td>
<td></td>
</tr>
<tr>
<td>bcc-cesm1-1-m</td>
<td>500</td>
<td>bcc-cesm1-1-m</td>
<td></td>
</tr>
<tr>
<td>Beijing Normal University</td>
<td>BNU-ESM</td>
<td>560</td>
<td>BNU-ESM</td>
</tr>
<tr>
<td>Canadian Centre for Climate Modelling and Analysis</td>
<td>CanESM2</td>
<td>1000</td>
<td>CanAM4</td>
</tr>
<tr>
<td>National Center for Atmospheric Research</td>
<td>CCSM4</td>
<td>1050</td>
<td>CCSM4</td>
</tr>
<tr>
<td>CESM1-BGC</td>
<td>500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CESM1-CAM5</td>
<td>300</td>
<td>CESM1-CAM5</td>
<td></td>
</tr>
<tr>
<td>Centro Euro-Mediterraneo per i Cambiamenti Climatici</td>
<td>CMCC-ESM</td>
<td>275</td>
<td></td>
</tr>
<tr>
<td>CMCC-CM</td>
<td>300</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CMCC-CMS</td>
<td>500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CMCC-CMS</td>
<td>850</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Centre National de Recherches Météorologiques</td>
<td>CSIRO-Mk3-6-0</td>
<td>500</td>
<td>CSIRO-Mk3-6-0</td>
</tr>
<tr>
<td>EC-EARTH consortium</td>
<td>EC-EARTH</td>
<td>450</td>
<td>EC-EARTH</td>
</tr>
<tr>
<td>LASG, Institute of Atmospheric Physics, Chinese Academy of Sciences</td>
<td>FGOALS-g2</td>
<td>700</td>
<td>FGOALS-g2</td>
</tr>
<tr>
<td>NOAA Geophysical Fluid Dynamics Laboratory</td>
<td>GFDL-CM3</td>
<td>500</td>
<td>GFDL-CM3</td>
</tr>
<tr>
<td>GFDL-ESM2G</td>
<td>500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>GFDL-ESM2M</td>
<td>500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NASA Goddard Institute for Space Studies</td>
<td>GISS-E2-H</td>
<td>240</td>
<td>GISS-E2-H</td>
</tr>
<tr>
<td>GISS-E2-R</td>
<td>550</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Met Office Hadley Centre (additional HadGEM2-ES realizations contributed by Instituto Nacional de Pesquisas Espaciais)</td>
<td>HadGEM2-ES</td>
<td>700</td>
<td></td>
</tr>
<tr>
<td>HadGEM2-CC</td>
<td>240</td>
<td></td>
<td></td>
</tr>
<tr>
<td>HadGEM2-CC</td>
<td>575</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Institute for Numerical Mathematics</td>
<td>inmcm4</td>
<td>500</td>
<td>inmcm4</td>
</tr>
<tr>
<td>Institut Pierre-Simon Laplace</td>
<td>IPSL-CM5A-LR</td>
<td>1000</td>
<td>IPSL-CM5A-LR</td>
</tr>
<tr>
<td>IPSL-CM5A-MR</td>
<td>300</td>
<td>IPSL-CM5A-MR</td>
<td></td>
</tr>
<tr>
<td>IPSL-CM5B-LR</td>
<td>700</td>
<td>IPSL-CM5B-LR</td>
<td></td>
</tr>
<tr>
<td>Japan Agency for Marine-Earth Science and Technology, Atmosphere and Ocean Research Institute (The University of Tokyo), and National Institute for Environmental Studies</td>
<td>MIROC5</td>
<td>700</td>
<td>MIROC5</td>
</tr>
<tr>
<td>MIROC-ESM</td>
<td>530</td>
<td></td>
<td></td>
</tr>
<tr>
<td>MIROC-ESM-CHEM</td>
<td>250</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Max Planck Institute for Meteorology</td>
<td>MPI-ESM-LR</td>
<td>1000</td>
<td>MPI-ESM-LR</td>
</tr>
<tr>
<td>MPI-ESM-MR</td>
<td>1000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Meteorological Research Institute</td>
<td>MRI-CGCM3</td>
<td>500</td>
<td>MRI-CGCM3</td>
</tr>
<tr>
<td>NorESM1-M</td>
<td>250</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NorESM1-ME</td>
<td>500</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
the MEM from the observations, in this case from the Global Precipitation Climatology Project (GPCP) [Adler et al., 2003]. Several aspects of the rainfall biases discussed in section 1 are readily apparent. For example, the MEM is too wet in the SH eastern Pacific, reflecting the model simulation of a spurious SH ITCZ there, while the dipole appearing along the poleward portion of the SPCZ is consistent with its too zonal orientation in the models. Along the equator, especially to the west of the International Dateline, the MEM considerably underestimates rainfall relative to GPCP, consistent with too cool SSTs and excessive westward extension of the cold tongue [Li et al., 2015, 2016]. Farther to the west near the Maritime continent, the CMIP5 models are excessively wet, as they also are over the western coast of South America. An important caveat in discussing these biases is that different observational products may yield divergent estimates of rainfall. For example, the GPCP estimates of precipitation are lower over much of the tropical and subtropical oceans, especially in the west Pacific, compared to the Climate Prediction Center Merged Analysis of Precipitation [Xie and Arkin, 1997] data set, which has been attributed to use of atoll-based rain gauge estimates in the latter but not in the former [Yin et al., 2004]. While differences across observational estimates are clearly important in validating model performance, for our purposes in understanding the spread of CMIP5 simulations relative to the MEM, they are not critical.

3.1.1. First PUP for DJF

For the PUPs computed from the $N=36$ coupled model DJF precipitation climatologies, the leading two modes emerge as well separated from the remaining modes and are significant according to the method of North et al. [1982]. The first mode, which accounts for 24.3% of the total field variance, is depicted in Figure 2a. The leading PUP predominantly captures the CMIP5 historic ensemble’s spread in the meridional width of principal centers of Pacific region deep convection. Within the SPCZ, the leading mode exhibits its largest positive loadings slightly equatorward of the mean diagonal axis through the mean precipitation centroid over 5°S to 15°S; the ITCZ is similarly split. The gray 4 mm d$^{-1}$ contours, representing averages over models with positive (solid) and negative (dashed) loadings (see Figure 2b), underscore the spatial displacements of the SPCZ and ITCZ between the two subsets of models.

Comparing the leading PUP to the MEM bias relative to GPCP (Figure 1b) indicates little systematic relationship between the spatial patterns. For example, along the poleward margin of the ITCZ and along the equator just west of the Dateline, the positive weight models have reduced bias compared to the models with negative weights. On the other hand, the models with positive weights exhibit an enhanced spurious SH ITCZ, which is especially evident in the 4 mm d$^{-1}$ contour. Such behavior underscores a difficulty in bias correction, namely, that alleviation in one region is often associated with degradation in another [Wang et al., 2014].

The Australian Community Climate and Earth System Simulator (ACCESS) and Hadley Centre Global Environmental Model version 2 (HadGEM2) families of models exhibit the largest positive model weights, corresponding to a narrower ITCZ/SPCZ complex with precipitation more concentrated along the equator, while the MPI models exhibit the largest negative weights, corresponding to a wider ITCZ/SPCZ. Overall, the model weights for simulations from the same parent are typically close. The effective degrees of freedom [Bretherton et al., 1999] estimated from the variance spectrum of the EOF modes is $\approx 9$. The tendency for similar values of model weights for sibling models is consistent with a lower number of degrees of freedom in the ensemble, since not all models within the ensemble are independent. However, it is not always the case that siblings are close; e.g., two of versions of the Institut Pierre-Simon Laplace (IPSL) models exhibit modest negative weights with respect to PUP 1, while the third has a positive weight. In this case, the two negative weight models share the same convection scheme (differing otherwise in terms of horizontal resolution), while the third has a distinct convection scheme [Oueslati and Bellon, 2013].

Obviously, it is necessary to assess whether the PUPs represent physically plausible behavior or are merely mathematical artifacts of the methodology: after all, it is possible that the spatial structure may have no clear relationship to underlying physical processes. To provide some physical context, we linearly regress various climate fields, including SST, winds at 850 mb and 200 mb, and specific humidity at 700 mb, from the models using the leading mode PC (model weights) as the regression index. Our objective is to relate these regressions to known thermodynamic and dynamic mechanisms, drawing analogies between how these mechanisms operate in producing observed (and simulated) behavior, such as interannual variability, and the spread inherent in the model ensemble.
Figure 2. First PUP of DJF-mean precipitation climatologies for the historic CMIP5 simulations. (a) The first PUP spatial pattern (EOF), in units of mm d\(^{-1}\). The solid and dashed contours represent the 4 mm d\(^{-1}\) isolines for models with positive and negative loadings of this spatial pattern, respectively. Stippled areas pass the bootstrap significance test at the 99% confidence level (see text). (b) Model weights (PCs) for mode 1, in units of standard deviation. The error bars represent the range of PC values that can arise from internal variability using model preindustrial control runs (see text). (c) Regression of the model's SST (shading) and 850 mb winds (vectors) based on the weights shown in (b) and scaled by 1 standard deviation. The vectors are plotted when the regression slope of at least one component passes a two-sided test for difference from zero at the 95% confidence level.
In Figure 2c, we present the results of the regression analysis for SST and 850 mb winds. The values shown correspond to unit standard deviation scaling of the PC, i.e., a model weight of +1. From the SST regression, the near-equatorial enhancement of rainfall for the leading PUP is associated with a widespread region of SSTs in the central to eastern Pacific ~0.5–0.75°C warmer than the MEM (again, scaled for a model weight of +1). These warm SSTs both underlie the enhanced rainfall and further extend to the east of the principal area of positive rainfall values evident in Figure 2a. The spatial patterns of rainfall and SSTs are qualitatively analogous to the behavior for interannual variability associated with El Niño/La Niña events in both observations and models [Folland et al., 2002]. Thermodynamically, the occurrence of warmer than MEM SSTs over a broad region upstream, as defined based on the orientation of the mean low-level trade wind inflow, is associated with higher low-level moist static energy (MSE), both through low-level warming and moistening. Thus, models with higher low-level MSE compared to the MME are expected to support rainfall further to the east [Lintner and Neelin, 2008; Niznik and Lintner, 2013], which is clearly evident in the more eastward position of the 4 mm d⁻¹ contour for positive weight models compared to negative weight models.

The leading mode 850 mb winds are associated with anomalous flow convergence along the SPCZ, coincident with the enhanced rainfall there. Moreover, within the SPCZ region, the 850 mb winds are anomalous northwesterly to westerly. Since the climatological DJF low-level circulation in this region is southeasterly to easterly, the 850 mb winds in models favoring higher rainfall along the equator are therefore weakened. Here we note the consistency with the physical mechanism for variability at the margins of tropical deep convection zones discussed by Lintner and Neelin [2008] and Niznik and Lintner [2013]. In particular, trade wind inflow from the relatively cool and dry southeast tropical Pacific represents a drying advective tendency that acts to suppress precipitation. With a slackening of the trades, drying advection in this region is reduced, supporting the eastward extension of SPCZ rainfall. Moreover, the principal axis of 850 mb winds along the SPCZ for models with positive weights coincides with enhanced rainfall extending southeastward toward SH midlatitudes; this behavior suggests export of tropical moisture along the SPCZ in these models that can sustain convection to the southeast. Further to the west along the poleward edge of the SPCZ, weak equatorward flow transports drier mean air masses into the SPCZ, which along with local cooling of SST is associated with reduced rainfall. In the extreme southeast Pacific, the low-level winds in Figure 2c are associated with an anomalous cyclonic circulation opposing the quasi-stationary climatological mean anticyclone (the South Pacific High) located there. Regressions of specific humidity at 700 mb and winds at 200 mb (not shown) also support these results.

An important distinction between the PUP analysis presented here and conventional EOFs calculated across a time series is that the PUP modes can arise from two sources of variance: internal climate variability in individual models and true intermodel variability. Prior work [e.g., Deser et al., 2012] indicates that internal variability can lead to distinct regional behavior in climatologies over time scales comparable to the 27 year means for our PUP analysis. For example, in the Pacific, models simulate well-known low-frequency modes of observed variability like the Pacific Decadal Oscillation (PDO) or the Interdecadal Pacific Oscillation (IPO), but the phase of these is dependent on the model initialization [Anderson et al., 2015]. Since the spatial footprint of the PDO (or IPO) on SST in the tropical and southern Pacific is somewhat reminiscent of the SST regression in Figure 2c, distinguishing between internal (sampling) variability and systematic intermodel variability requires careful attention, and we have addressed this in three separate and complementary ways.

First, we employed a bootstrapping technique to provide a significance test for the pattern in Figure 2a. This was done by generating 100 randomized 30 year climatologies from 5 year segments in the preindustrial control runs (see Table 1 for more information). This procedure yielded 100 “alternative” ensembles, and a PUP analysis was performed on each. The average spatial correlation between the leading modes from this set of 100 alternative ensembles and that in Figure 2a is \( r = 0.95 \), implying that the pattern seen in Figure 2a is robust to sampling. A two-sided \( t \) test was further applied at each grid point to these modes to assess whether the sample means of grid point values among the 100 bootstraps are significantly different from zero. The results of this test are stippled where grid points pass at the 99% confidence level in Figure 2a, indicating widespread confidence that the leading mode does not arise from sampling of interdecadal variability.

As a second check that the results in Figure 2a are not the result of internal variability, we calculated the climatology of the preindustrial control run simulation for each model over its entire length (ranging from 240 to 1050 years); that is, we check whether the spatial pattern seen in Figure 2a is reproducible for
climatologies much longer than 30 year averages. The spatial correlation between the first PUP EOF for the climatologies computed from these lengthier preindustrial control integrations (not shown) and the 1979–2005 climatologies is \( r = 0.95 \), with similar percent variance accounted for, indicating that the PUP behavior is further distinct from sampling across low-frequency oscillations on the order of 100 years or longer.

A final test can be seen in the error bars in Figure 2b. Consecutive, nonoverlapping 30 year climatologies from the preindustrial control runs were calculated for each model, and the resulting climatologies were centered by the 1979–2005 ensemble mean and projected onto Figure 2a. The error bars in Figure 2b represent the range of values for these projections or a measure of internal variability of the principal components. The spread for each model is notably smaller than that across the entire ensemble, indicating that internal model variability is not a major contributor to the pattern in Figure 2a.

Taken together, this set of checks leads us to conclude that the PUP in Figure 2a represents true systematic differences across model climatologies, distinct from internal model variability.

### 3.1.2. Second PUP for DJF

The second mode PUP for the historic ensemble, accounting for 16.9% of the field variance, is presented in Figure 3. The predominant feature of this PUP is widespread occurrence of positive values outside of the central and eastern Pacific, with especially large values in the SPCZ and to the north of Australia (Figure 3a). By contrast, the second PUP reflects strong negative values over the spurious SH ITCZ as well as in the upwelling region adjacent to the coast of South America. The spatial trade-off in precipitation intensity between the SPCZ and ITCZ can be interpreted qualitatively in terms of a teleconnected atmospheric response to diabatic (convective) heating, as in the Gill [1980] model. That is, those models which exhibit stronger convection over the SPCZ may be expected to simulate weaker precipitation elsewhere (such as over the eastern Pacific) through mass balance of stronger ascent in the SPCZ and stronger subsidence elsewhere. We point out that the areas enclosed by the 4 mm d\(^{-1}\) contour are approximately the same for both the positive and negative weight models, which is consistent with the notion of a spatial redistribution of rainfall within the domain. The regression analysis (Figure 3c) highlights SSTs colder than the MEM collocated with the largest negative rainfall values in the eastern tropical Pacific.

Our leading PUP modes are in general agreement with the results of LX14 (cf., their Figure 2), which depict regressions of precipitation, SST, and surface winds onto PCs of intermodal spread in annual- and zonal-mean tropical Pacific rainfall, normalized with respect to each model’s tropical mean rainfall, for a smaller set \((N = 18)\) of CMIP5 models. LX14 remark that similar results were obtained for the decomposition over longitude and latitude, which would be more directly comparable to our analysis. There are, however, some differences with respect to LX14. For instance, the leading PUP from our analysis accounts for less than half the variance compared to the leading mode of LX14. This difference may stem from the normalization applied in LX14, which may be expected to suppress some of the spread across models, given model-to-model differences in the overall amount of tropical rainfall, thereby increasing the variance captured by the leading mode in LX14. The second mode of LX14 manifests a much more pronounced zonal dipole in the regression of precipitation over the eastern north tropical Pacific than is evident in our second mode; we will further address this behavior in the context of our results for June-July-August (JJA) below. Overall, though, the similarity of the leading PUPs to the results of LX14, obtained with some differences in the underlying methodology and selection of models and analysis period, supports the robustness of these patterns of model spread.

As with the leading mode, we checked the reproducibility of the pattern in Figure 3a against sampling variability: using the bootstrap method, the spatial correlation between 100 bootstrapped second PUP modes and that of Figure 3a is \( r = 0.94 \). The stippling throughout Figure 3a underscores that the behavior at most grid-points is distinct from internal variability, and the small error bars on model weights in Figure 3b show that within-model spread is small compared to the spread across the ensemble. Finally, the second PUP EOF calculated from the climatologies based on the longer preindustrial control runs is spatial correlated with the second PUP EOF for 1979–2005 at \( r = 0.94 \), again underscoring that the 1979–2005 period is sufficient for examining the model spread. We therefore reiterate that the second mode is distinct from sampling internal variability at decadal or longer time scales.

It is interesting to note that while the first and second PUP PCs are uncorrelated in a linear least squares sense (by construction), they do exhibit an apparent higher-order relationship (Figure 4). In particular, using a
The quadratic fitting function yields a correlation of 0.54 between the two PCs. Rejecting the obvious outliers (the Commonwealth Scientific and Industrial Research Organisation (CSIRO), Centro Euro-Mediterraneo per i Cambiamenti Climatici-Community Earth System Model-Coupled Modeling System (CMCC-CMS), and CMCC-Community Earth System Model (CESM), Goddard Institute for Space Studies (GISS) models) further increases the quadratic best fit ($r = 0.78$) without significantly altering the linear correlation. The quadratic relationship between the model weights for the first two modes implies that models with strong SPCZ regional rainfall (second PC > 0) may have either relatively narrow (PC > 0) or wide (PC < 0) meridional...
distributions of rainfall, while models with weak SPCZ region rainfall tend to fall closer to the ensemble-mean with respect to the overall latitudinal extent of Pacific region convection.

3.1.3. PUPS for JJA
As we noted in section 2, our study emphasizes DJF, when the SPCZ is of strongest intensity. Of course, it is worthwhile to consider how the results for DJF compare to other seasons. Thus, we provide here a brief summary for a PUP analysis of the mean precipitation climatologies averaged over austral winter (June-July-August or JJA). Figure 5 illustrates the EOFs of the two leading modes of precipitation spread computed for JJA. Structurally, the first PUP EOF for JJA (Figure 5a) manifests some similar elements to the EOF for DJF (Figure 2a); e.g., values are higher near the equator and lower on the poleward edges of the ITCZ/SPCZ complex. Given the much less prominent SPCZ in JJA and the presence of dry monsoon conditions over northern Australia, the largest values for first JJA mode are more confined to the Northern Hemisphere; indeed, the spatial pattern is broadly translated northward compared to DJF, consistent with the seasonal migration of convection. The 850 mb wind anomalies for a model weight of +1 standard deviation are also more confined to the Northern Hemisphere in JJA. Despite the spatial resemblance of the leading EOFs for DJF and JJA, correlating the model weights for JJA (not shown) with those for DJF yields a modest positive correlation ($r = 0.52$). Thus, we conclude that there is some variation in the relative contributions of individual models to producing the leading mode of uncertainty between DJF and JJA, even as the spatial patterns are comparable.

Although the second EOF for JJA (Figure 5b) also bears similarity to the second EOF for DJF (Figure 3a), the former features a pronounced zonal dipole over low NH latitudes of the central and eastern Pacific. In fact, this dipole supplants the uncertainty trade-off in the SPCZ-spurious ITCZ as the dominant feature in mode 2. Also, as we discussed in the previous subsection regarding the comparison of our results to LX14, the presence of the strong zonal dipole in JJA is more consistent with the behavior seen in LX14’s second mode for the annual mean, indicating that in this region, the model spread in JJA imprints strongly on the annual mean. Somewhat surprisingly, the model weights for JJA and DJF are more strongly correlated ($r = 0.84$) for the second mode compared to the first, despite less apparent spatial coherence of the EOFs. Thus, it appears that the mechanisms responsible for the second mode of CMIP5 model spread produce seasonally distinct spatial loci of strong uncertainty but do so with a similar ordering of the model weights.

3.2. MCA and Relationship of Coupled Model Precipitation Spread to SST
As noted above, within coupled models, biases are often attributed to poor simulation of ocean dynamics. With respect to simulated precipitation, errors arising from ocean dynamics may impact SSTs, which in turn induce errors in surface fluxes and ocean-atmosphere coupling that affect temperature and moisture vertical structure in the overlying atmosphere. To investigate this linkage, we applied Maximum Covariance Analysis (MCA) to the cross-covariance matrix of normalized precipitation and SST for the historic simulations, as shown Figure 6. The leading MCA mode accounts for 66% of the total squared covariance between these two fields, with a correlation coefficient between the model weights for the precipitation and SST fields of $r = 0.79$, implying tight coupling between the model spread in precipitation and SST. The squared covariance value is significant at the 94% confidence interval, based on a Monte Carlo procedure with a sample size of 300. The precipitation pattern associated with the spatial projection of the first MCA mode manifests a horseshoe-like pattern reminiscent of the leading coupled PUP mode in Figure 2a; in fact, the spatial pattern
The correlation coefficient between the leading coupled model EOF- and MCA-based PUPs is 0.78, while the model weights for these PUPs are correlated with $r = 0.88$. One difference in the precipitation field of the MCA-based PUP relative to the first EOF-based PUP is that the former exhibits large values in the vicinity of the spurious SH ITCZ (around 120°W, 10°S); in this regard, the leading SVD precipitation pattern more resembles the second EOF-based PUP. Indeed, the spatial correlation pattern coefficient ($r = 0.35$) and the correlation of model weights ($r = 0.32$) for the second precipitation EOF PUP and leading MCA PUP are both significant at $p = 0.05$.

### 3.3. PUPs for AMIP-Style Simulations

We have also analyzed the spread across ensemble members for the AMIP-style simulations. Analogous to Figure 1, Figure 7 depicts the DJF MEM precipitation for the AMIP ensemble as well as the bias relative to GPCP. Overall, there is an improved spatial distribution of precipitation over the domain, with the spurious SH ITCZ effectively eliminated and the slope of the SPCZ improved, although the tilt of the more subtropical portion is still somewhat too zonal. Also, the intensity of rainfall within the SPCZ and ITCZ is generally larger than the GPCP values. Interestingly, in comparison to the coupled models, the bias actually worsens along the northern margin of the extreme eastern portion of the ITCZ: a possible explanation for the degradation of the AMIP simulations in this region is that competition for convection between the NH and SH ITCZs in the coupled simulations suppresses intensity to the north, leading to values more in line with GPCP.
For the AMIP-style ensemble, the spread across ensemble members arises from poor parameterizations or missing physics within the atmosphere only, since the same boundary conditions (SSTs and sea ice) are prescribed across the models. A gross comparative measure of the total variability within that selection of models for each of the historic and AMIP-style ensembles can be obtained from the sum of squares of the elements in the covariance matrix (the Frobenius norm [see Bretherton et al., 1992]), which we normalize by the number of models in each ensemble to account for the different number of models. For the coupled ensemble, the (normalized) Frobenius norm is ~1855 mm$^2$ d$^{-2}$, while it is ~1190 mm$^2$ d$^{-2}$ for the AMIP-style simulations. The larger intermodel variability within the coupled ensemble is consistent with additional sources of uncertainty owing to coupling of the atmosphere to an interactive ocean. Nevertheless, that the total variance in the AMIP models is ~2/3 as large as in the fully coupled versions indicates that atmospheric processes alone contribute substantially to ensemble spread.

Figure 8 presents the leading EOF-based PUP for the AMIP-style simulations. This mode explains 23.4% of the total variance, i.e., comparable to mode 1 for the historic ensemble. For the AMIP PUPs, only the leading mode is well separated from the remaining modes. Overall, the leading AMIP PUP spatial pattern highlights model discrepancies localized primarily over the western portion of the domain where simulated precipitation values are largest: models with positive loadings exhibit larger than MEM rainfall over the SPCZ and lower values to the north in the ITCZ as well as over northern Australia. The latter region is characterized by a summer monsoon climate. Prior work [e.g., Kiladis et al., 1989; Mantsis et al., 2013] points to coupling with the Australian summer monsoon as an important determinant of SPCZ intensity and spatial structure, especially in its more tropical portion. This linkage is consistent with the structure in the leading PUP, in that models with enhanced precipitation in the SPCZ tend to simulate reduced precipitation in the Australian monsoon region. As with the leading mode of the coupled ensemble, the regression of model weights for the leading AMIP PUP onto 850 mb winds indicates stronger (north)westerlies in models with more intense rainfall in the SPCZ.

Relative to the historic coupled ensemble, the MEM DJF 4 mm d$^{-1}$ precipitation for the AMIP-style simulations more closely approximates the location of the observed 4 mm d$^{-1}$ contour, demonstrating improved fidelity among the AMIP-style simulations in capturing the overall spatial distribution of precipitating deep
convection in the Pacific domain. That is, the specification of the boundary forcing through imposed SSTs leads to a better match to observed rainfall distribution. The spatial pattern correlations of the leading AMIP PUP modes with respect to the first and second historic EOFs are 0.63 and 0.22, respectively. Thus, errors or uncertainties in simulations of the atmosphere itself may be viewed as contributing to the spatial pattern of the leading coupled mode, in addition to the structural differences associated with fully coupled ocean-atmosphere dynamics. Some caution is warranted in comparing the results, given the different models assessed in the coupled and AMIP-style simulations. Still, for the subset of models common to both the coupled and AMIP-style ensembles (N = 25), the correlation between model weights of the leading PUPs is 0.49, which is significant at p = 0.05. This correlation remains significant at the 95th percentile even if reasonable allowance is made for a lower number of degrees of freedom owing to nonindependent models.

3.4. PUPs for Precipitation Standard Deviation

In addition to computing PUPs for the DJF precipitation climatologies, we have also calculated PUPs with respect to simulation of the interannual DJF standard deviation in the coupled simulations. Our interest in computing PUPs on interannual standard deviation is principally to illustrate the applicability of the PUP approach to other dimensions of precipitation besides climatological means, which are frequently the focus of model intercomparison studies. However, as numerous studies [e.g., Russo and Sterl, 2012; Huang et al., 2013; Toreti and Naveau, 2015] have demonstrated, uncertainties in precipitation means may be quite distinct from other aspects of precipitation behavior such as extremes. Thus, multimodel evaluation should take into account these potential differences.

The two leading standard deviation PUPs (Figure 9) account for 30.3% and 16.9%, respectively, and are well separated from the remaining modes. The first PUP EOF (Figure 9a) is effectively of the same sign across the

Figure 7. As in Figure 1 but for the 30-member AMIP-style ensemble.
Pacific region; thus, for this mode, models tend to exhibit either higher or lower variability relative to the MEM ubiquitously throughout the domain. As with the PUPs for DJF mean rainfall, the weights of models in the same family tend to lie close to one another, though again, the IPSL family of models contains both low and high variance versions differing by convection scheme. Also notable are the two earth system models (ESMs) from Geophysical Fluid Dynamics Laboratory (GFDL), which differ principally in the formulation of their ocean components: GFDL-ESM2M exhibits much higher variability than GFDL-ESM2G, which may be due to the latter having relatively low mean rainfall in the equatorial region (see Figure 2a).

The second mode EOF (Figure 9b) points to models with enhanced interannual variability along the equator, especially concentrated in the central Pacific, and reduced variability in surrounding regions. The localization of the largest values of the second PUP EOF to the central equatorial Pacific suggests spread arising from model simulation of ENSO and atmosphere-ocean feedback within this region. CMIP5 models have been shown to display a wide range of skill in simulating aspects of ENSO such as its frequency of occurrence, intensity, and spatial structure, though few models score uniformly well on all characteristics [Bellenger et al., 2014]. One of the problematic aspects is the simulation of distinct eastern Pacific- and central Pacific-type El Niño events, with CMIP5 models often failing to simulate, or undersimulating, the latter [Fang et al., 2015]. For the second PUP model weights, there is a modest ($r = 0.4$) correlation with NINO3 region SST variability: although suggestive of a relationship between the second PUP and ENSO, a more rigorous exploration is clearly warranted. Because of uncertainties in the spatial characteristics of ENSO simulation, for instance, NINO3 may not represent the optimal index for comparison.

Figure 8. First PUP of DJF-mean precipitation climatologies for the AMIP simulations. (a) The first PUP spatial pattern (EOF), in units of mm d$^{-1}$. The solid and dashed contours represent the 4 mm d$^{-1}$ isolines for models with positive and negative loadings of this spatial pattern, respectively. (b) Model weights (PCs) for mode 1, in units of standard deviation. The vectors correspond to the regression of 850 mb winds on the weights shown in Figure 8b.
Perhaps not surprisingly, the model weights for the historic ensemble means and standard deviations exhibit some relationships. Both the first and second PUP model weights for the historic climatology are positively correlated with the model weights of the leading PUP for standard deviation; i.e., the models exhibiting more intense climatological precipitation along the equator and/or along the SPCZ tend to be those with higher interannual standard deviations; i.e., areas with higher mean rainfall experience a greater degree of year-to-year variability. On the other hand, model weights for the second historic climatology PUP are negatively correlated with those of the second standard deviation PUP; i.e., models with higher rainfall interannual variability over the equatorial central Pacific tend to have a more pronounced climatological double ITCZ, but less intense rainfall in the core of the SPCZ.

For completeness, we have further computed PUPs on the DJF interannual precipitation standard deviation for the AMIP-style simulations (not shown). The leading mode, which accounts for 38.4% of the variance, strongly resembles the leading mode for the historic ensemble (Figure 9a), again showing pervasive differences across the models in the overall level of precipitation variability and pointing to uncertainties in representation of atmospheric processes as the principal determinant of this aspect of model spread. On the other hand, no analogue to the historic ensemble second mode standard deviation PUP (Figure 9b) is evident in the AMIP-style ensemble, which underscores the role of ocean-atmosphere coupling in generating this aspect of the interannual variability in the CMIP5 models.

4. Summary and Discussion

In this study, we have applied an approach, generically termed principal uncertainty pattern (PUP) analysis, to investigate the leading patterns characterizing the spread among CMIP5 model simulations of tropical Pacific precipitation. For DJF, the two leading PUPs for the historic (coupled ocean-atmosphere) simulations, derived from EOF/PC analysis, reveal distinct patterns of differences of the models with respect to ensemble mean in both the spatial distribution of precipitation as well as its intensity. The first mode can be broadly characterized in terms of spread in the meridional width of the Pacific ITCZ-SPCZ complex as well as the zonal distribution of precipitation along the equator. The second mode shows spread expressed as a trade-off between SPCZ and ITCZ precipitation intensity, the latter including the spurious SH ITCZ. Broadly similar modes are
evident for JJA, but for the first mode, the strongest signals are displaced northward, consistent with the mean seasonal migration of tropical convection from DJF to JJA, while for the second mode, the dominant signature is a zonal dipole in precipitation spread over low latitudes in the NH eastern Pacific.

As we have noted, PUPs may reflect either true intermodel spread or internal variability, which is quite distinct from application of EOFs (or other methods) in the time domain. Thus, an important consideration is how to distinguish these two potential sources of PUP behavior. To address this, we performed a bootstrap significance test for the intermodel spatial patterns, a test on the model weights, and a check for robustness against longer climatological averages. The results confirm in complementary ways that these patterns, in fact, arise from intermodel differences in the tropical Pacific climatology and are distinct from internal model variability at times scales of several decades or longer.

Simple linear regressions of SST and low-level circulation (as well as upper level circulation and specific humidity) onto precipitation PUP model weights underscore the physical consistency of these interpretations, as does application of maximum covariance analysis (MCA) to the covariance matrix of precipitation and SST. By analyzing the stand-alone atmospheric (AMIP-style) simulations in which the impacts of SST-related biases are suppressed, intermodel spread in rainfall intensity remains, especially in the western tropical Pacific, even as the overall spatial configuration of domain-wide precipitation is improved.

While we have demonstrated the physical consistency of the precipitation PUPs with the spread inherent in other climate fields, can we draw any conclusions about the source of spread as it relates to particular aspects of model parameterizations, especially for the AMIP-style models for which errors related to ocean dynamics are suppressed? One way of viewing the spatial structure inherent to the leading AMIP PUP (Figure 8a) is that represents a trade-off between precipitation in the SPCZ core compared to the margins; i.e., models with more intense precipitation in the SPCZ core have narrower SPCZs. In prior work using an intermediate level complexity model, Lintner et al. [2012] described a pattern of reduced precipitation along the margins and enhanced precipitation in the cores of strong tropical convection zones with the addition of an entrainment-like process to the model’s convection scheme. The occurrence of this spatial pattern was tied to dry air mixing reducing convective available potential energy along the margins with enhanced precipitation in the interior related to enhanced moistening available via large-scale convergence within the convection zone core. Oueslati and Bellon [2013] documented similar behavior in entrainment sensitivity experiments in the family of Centre National de Recherches Météorologiques (CNRM) models, as did Hirota et al. [2014] in Model for Interdisciplinary Research On Climate version 5 (MIROCS) simulations with different representations of entrainment.

It remains to be seen whether the PUP model weightings can be systematically related to entrainment or other parameterized processes. On this note, Siongco et al. [2014] applied an object classification method to sort CMIP5 AMIP-style models into two groups, depending on where these models exhibited the strongest bias in the Atlantic ITCZ; they uncovered no systematic relationship between the location of bias and the convective parameterization used. A practical challenge is that comprehensive documentation of parameter values for CMIP5 models is difficult to obtain. We did examine model weightings for the first AMIP PUP with respect to qualitative descriptors of model components available from the Earth System Documentation website (http://compare.es-doc.org/), but this indicated no obvious candidates for attribution of model spread.

Moving forward, we anticipate continuing application of PUPs as a tool for diagnosing sources of model ensemble spread in precipitation and how these relate across different variables. For example, Bellucci et al. [2010] and Oueslati and Bellon [2015] have speculated that overestimation of the occurrence frequency of weak or moderate ascent regimes in the CMIP5 ensemble, rather than precipitation intensity within different vertical velocity regimes, principally accounts for the simulated precipitation errors in these models. Thus, inclusion of the vertical motion field in the MCA may be instructive. We also envision application of PUPs to single model ensembles in which a parameter or set of parameters is systematically varied. In recent work, Bernstein and Neelin [2016] used a perturbed physics ensemble of the Community Earth System Model to demonstrate how the introduction of variation across parameters in convection schemes can significantly alter regional precipitation responses to global warming. By analyzing such simulations using PUPs, we can quantify the extent to which systematic variations in single or multiple parameters may contribute to distinct spatial patterns of model disagreement.
References


